Abstract

We discuss the problem of 2D+t intra- and inter-sequential registration of retinal angiograms. A joint spatio-temporal registration algorithm is presented based on a RANSAC approach incorporating a quadratic model to describe "pairwise" image homography. This is incorporated into a local-to-global hierarchical joint registration framework. After registration, vessel centrelines are segmented by applying multi-scale steerable complex wavelet filters to detect vessel centrelines to subpixel accuracy. Frame-by-frame microvascular centrelines in Regions-of-Interest (ROIs) are evaluated against segmented centrelines of the temporal average of the registered sequences. The microvascular centrelines in registered sequences can be compared intra-sequentially and inter-sequentially for clinical applications, for the non-invasive comparison and monitoring of micro-circulation. This has the potential to detect the presence of microemboli and pathological structural alterations.

Introduction

The retinal vascular system has spawned a huge range of clinical and pre-clinical research and diagnostic techniques since it provides unique in vivo access for studying the characteristics of the human vascular bed in a minimally invasive manner.

Fluorescein angiography is a well-established technique for clinical assessment of the retina. The passage of fluorescein dye through the retinal vessels reflects both the vessel structure and the rate of retinal blood flow. A fundus camera continuously photographs the retina from the onset of dye injection over a period of 3 to 5 minutes [1]. This captures filling (“wash-in”) and the subsequent elimination (“wash-out”) of dye in the retinal vessels. These angiogram sequences are roughly divided into the arterial phase (filling of retinal arteries), arteriovenous phase (complete filling of retinal capillaries with laminar flow exhibited in retinal veins), venous phase (complete filling in large retinal veins, leading to the maximum vessel fluorescence) and recirculation phase (approximately equal brightness in the veins and the arteries, gradual elimination of dye from the retinal vasculature).

Measurements on retinal blood vessels have linked alteration of human (retinal) vasculature with diseases such as hypertension, diabetes and age-related macular degeneration [2]. For early stage detection, subtle changes in the retinal microvasculature require sufficiently fine-resolution imaging and dependable sub-pixel precision of registration to study vessels at the micrometer scale. Current literature focuses on establishing correspondence between global microvascular measures and retinal blood flow [3]. Suggested parameters are blood flow velocity, arteriovenous passage time, difference of arterial and venous times to maximum intensity, and time to maximum image [3]. All of these fail to capture microvascular vessels individually.

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Blauth et al. [4] first suggested that comparison of pre- and post-operative retinal fluorescein angiograms might indicate the existence of microemboli that could be associated with cognitive impairment or even morbidity. However, only the macula region of one pre-op and one post-op image were used [4].

The analysis of sequential retinal angiograms has not been widely exploited; the dynamics of blood flow and the diffusion of the injected tracer introduce a low-frequency variation that is both difficult to compensate for and computationally demanding. However, fluorescein angiography allows visualisation of the microvasculature less than 30µm in diameter, which is not yet achievable by either funduscopy or color photography. By recruiting all frames in both sequences, it is possible to study retinal microvasculature dynamics and identify small, but potentially significant embolic events. In this paper, we address and solve three technical problems.

**Image registration** We need to estimate and model the distortion between frames in order to map each angiogram onto one common coordinate system (the reference). Current feature-based methods include global weak affine model with Bayesian matching [5], hierarchical model refinement [6] and dual-bootstrap iterative closest point (DB-ICP) [7]. Often, vascular bifurcation points are extracted as landmark points to estimate the transformation model. Inaccurate landmarks can heavily distort the transformation estimate, especially in [6], where each image only contains about 30-50 landmarks. This is improved in [7], where landmarks in local “bootstrap” regions are iterated over to establish correspondence and to fit and refine the transformation estimate. This method also relies on the accurate initialization of corresponding landmark points.

**Objective validation** We need an objective error measure to evaluate the performance of our registration algorithm. Registration error can be determined by the extent of misalignment between the registered image and the reference image. Conventional ground truth is obtained from manual registration [5]. This form of reference standard is subject to inter- and intra-observer variability. Therefore, [6] & [7] use the “centreline” (linked lines between landmarks) locations of the original images as relatively “unbiased” ground truth. However, both the linking algorithm that interpolates subpixel locations and the similarity measure that optimally matches subpixels between different frames vary from case to case in establishing error metrics. Therefore, [8] casts an evenly spaced virtual grid that intersects with vessels to obtain ground-truth pixels. This, however, disregards the location-dependent nature of pixel information. Pixels located near the capillary-rich macula region generate significantly more clinical interest than those near the retinal border (field-stop). Furthermore, their proposed “error tracing” route theoretically favors strategies that pair both the forward and the inverse registration functions to optimize the “net offset” rather than a true assessment of the registration algorithm on its own. Additional processing is required to address the uneven global illumination.

**Vessel segmentation** We need to differentiate and identify microvascular segments from the background in each of our angiograms. Exhaustive research focused on this area includes: use of morphology with Laplacian-of-Gaussian filtering [5], exploratory vessel tracing [6], region-growing on Hessian matrix maxima in scale-space [9] and maximum likelihood estimates from multi-scale filter output in scale-space [10]. Yet, most algorithms are developed on fundus images, and are not necessarily able to capture capillaries in fluorescein images at a much finer scale.

**Methods**

**Pairwise Image Registration** Geometric distortion, radiometric degradation, and additive noise corruption contribute to the difficulty in registration. Problems specific to clinical
retinal angiography are: the photographer’s bias in image capture, the patient’s involuntary movement, and the 3D to 2D warping between retina and the camera. Existing techniques, for example, approximate the retinal surface by a sphere [6], predict a perspective distortion [8], or model the intensity variation to address uneven illumination [11].

At the pairwise level, we combine projective RANSAC [12] with a quadratic homography transformation, pre-conditioned by contrast-enhancement within the field-stop. The latter is required because the low dye concentration in the retinal blood vessels both at the beginning and the end of the sequence requires temporary adjustment of the dynamic range of pixel intensities. To disregard the edge of the frame and the patient record information, a circular Hough Transform is used to detect the field stop. Local contrast within the field-stop is histogram equalized and vessel bifurcations or crossings (landmark) points are detected. False corners near the borders are eliminated with a distance criterion. Landmarks are then putatively matched by windowed normalized cross-correlation. RANSAC iteratively estimates the “best-fit” projective model applicable to most putative matches. We use the inliers-to-outliers ratio (the comparison between number of pairs that can be described by the “best-fit” model within offset threshold and those that cannot) as a criterion on whether to apply a higher order quadratic transformation model (with 12 degrees of freedom). Although the quadratic model is more tolerant to pairwise distortion, the refinement is only sensible if the lower order registration has been successful.

**Joint Registration** To analyse temporal information both within a consecutive sequence of retinal angiograms (intra-sequence) and across two different sequences taken before and after the operation (inter-sequence), we need a stepwise systematic framework that first aligns each pixel intra-sequentially then cross-aligns the same pixel inter-sequentially. Multitemporal registration requires maximizing the point correspondence between similar structural features, while still allowing us to differentiate, detect or even monitor pathological changes. For each patient, the last post-op frame was acquired several hours after the first pre-op frame. This increases the chance for the vasculature to alter both in width and in curvature, in addition to the natural variability of blood vessels.

For the $n^{th}$ frame in a sequence $S$ of length $N$, let $(x_n, y_n)$ denote the location in the frame coordinates at time $t_n$. The image is denoted by the function $f_n := f_n(x_n, y_n; t_n)$, $n \in [1, N]$.

Consider two unregistered angiogram sequences, acquired with frame-specific spatial coordinates relative to the camera lens, at unknown points in time relative to the cardiac cycle, and with non-uniform frame-to-frame intervals (from less than a second to tens of seconds) along each sequence: $S^{(A)} = \{ f_n^{(A)} \}_{n=1,2,3...N_A}$ and $S^{(B)} = \{ f_n^{(B)} \}_{n=1,2,3...N_B}$. We first spatially register each individual image $f_n^{(A)}$ in $S^{(A)}$ to a local reference spatial coordinate system defined by frame $f_{lr}^{(A)}$. This individual-to-local reference registration is also applied to sequence $S^{(B)}$ with frame $f_{lr}^{(B)}$ as its local reference. We then register the two local references $f_{lr}^{(A)}$ and $f_{lr}^{(B)}$ separately to one global reference $f_{gr}$. This local-to-global reference transformation is further combined with prior individual-to-local reference transformation to give the individual-to-global reference transformation that allows both $S^{(A)}$ and $S^{(B)}$ to be co-registered to one global reference $f_{gr}$.

We adopt the clinical practice of selecting the darkest image as the local reference. Our algorithm computes the sum of the pixel intensities within the field-stop and selects the frame at the peak of the dye-time course (when the image is the darkest) in each sequence: $f_{lr} = \{ f_n^{*} \}$, where $n^{*} = \arg \min_{n \in [1,N]} \langle f_n, M_n \rangle$, with $\langle \cdot, \cdot \rangle$ denoting a spatial inner product and $M_n$ a spatial weighting function (binary mask) that is unity for points $(x_n, y_n)$ within the field-stop.
The **individual-to-local reference** registration can be written as: \( f'_{n} = R_{n(\text{lr})}(f_{n}) \), where \( f'_{n} := f'_{n}(x'_{(\text{lr})}, y'_{(\text{lr})}; t_{n}) \), \( n \in [1, N] \) is the registration result when individual frame \( f_{n} \) is mapped to the spatial coordinate system of local reference \( f_{\text{lr}} \) by function \( R_{n(\text{lr})} \).

The **local-to-global reference** transformation can be written as: \( f''_{\text{lr}} = R_{\text{lr}(\text{gr})}(f_{\text{lr}}) \), where \( f''_{\text{lr}} := f''_{\text{lr}}(x''_{(\text{gr})}, y''_{(\text{gr})}; t_{\text{lr}}) \) is the registration result when the local reference \( f_{\text{lr}} \) is mapped to the spatial coordinate system of global reference \( f_{\text{gr}} \) by function \( R_{\text{lr}(\text{gr})} \).

Lastly, **individual-to-global reference** registration can be combined as: \( f''''_{n} = R_{\text{lr}(\text{gr})}(f''_{n}) \), where \( f''''_{n} := f''''_{n}(x''''_{(\text{gr})}, y''''_{(\text{gr})}; t_{n}) \), \( n \in [1, N] \) is the registration result when individual frame \( f_{n} \) is mapped to the spatial coordinate system of the global reference \( f_{\text{gr}} \).

### Vessel Segmentation

The estimate for the centreline location of the vessels requires sub-pixel resolution accuracy. In practice, fine vessel structure may not be captured in all frames within a sequence. It is commonly observed that capillaries may “disappear” from the previous frame then “re-emerge” in the following one. Lastly, due to the time delay in the passage of dye, angiograms at the beginning and end of a sequence contain significantly less information on the detailed microvasculature.

To take into account previous and subsequent frames in one or more sequences, the temporal average of the registered sequence(s), defined by: \( \bar{f}_{\text{average}} = \frac{1}{N} \sum_{n=1}^{N} f''''_{n} \)

is a more perceptually accurate representation of the retinal microvasculature. Our segmentation algorithm uses prior work [10], [13] and [14]. We apply steerable complex wavelet filters at multiple scales on each frame \( f_{n} \), and use the filter outputs to infer the presence of vessels and centreline locations.

A local orientation map can be constructed as: \( O^{(l)}_{n}(x_{n}, y_{n}) = \sum_{k=0}^{K/2-1} g^{(l)}_{k}(x_{n}, y_{n})e^{2\pi i k/p} \) for \( g^{(l)}_{k}(x, y) \), \( k = 0, 1, 2, ..., K - 1 \) denotes the output of the \( k^{th} \) order oriented bandpass complex analysis filter from image \( f_{n} \) at level \( l \), and \( p \) is a conditioning constant [13].

A local phase estimate, \( \Psi^{(l)}_{n} \), is obtained from filter steering by the polynomial functions \( s_{p}(\phi, k) \) and \( s_{q}(\phi, k) \) on \( f_{n} \): \( \Psi^{(l)}_{n} = \angle \left( \sum_{k=0}^{K/2-1} s_{p}(\phi, k)f^{(l)}_{k}(x_{n}, y_{n}) + \sum_{k=0}^{K/2-1} s_{q}(\phi, k)(f^{(l)}_{k}(x_{n}, y_{n}))^{*} \right) \).

For each pixel, we match local orientation \( O^{(l)}(x_{n}, y_{n}) \) with phase estimate \( \Psi^{(l)} \) in a 8-connected neighbourhood. The extracted centreline locations are refined by the subpixel information held in the phase shift between pixels. In scale-space, we link and weight the candidate locations at different scales to filter out the noise.

### Objective Validation

For validation, we take a patch (ROI) near the macula region with a high density of microvasculature. First, we establish our ground-truth as the centrelines \( v_{\text{average}}(x, y) \) within the ROI on \( \bar{f}_{\text{average}} \). Then we segment the vessel centrelines \( v_{n}(x, y) \) (within the same ROI) frame-by-frame in the co-registered pre- and post-op sequences. Comparing the centreline locations from each individual frame against ground-truth, we define the centerline error measurement (CEM), for a given ROI area with vessel length \( L \), as:

\[
\text{CEM} = \frac{1}{L} \sum_{n=0}^{L-1} \| v_{n}(x, y) - v_{\text{average}}(x, y) \|
\]

where \( \| \cdot \| \) is the Euclidean distance. This is a fairer assessment of registration quality as the clinically interesting fine-scale microvasculature contribute more strongly to the error metric than a spatially-averaged global measure.

### Experiments

We tested our proposed method on 384 retinal angiograms (4288-by-2848 pixels per frame, captured by a Zeiss retinal camera at 30 degrees field) from 6 patients. Each patient has
one pre-op and one post-op sequence, with $\sim 65$ frames per sequence. We processed our sequences using MATLAB 2009 on an Intel Dual Core CPU with 3.48G RAM. Our segmentation evaluation used ROIs of size $101 \times 101$ pixels near the macula containing complex orientations, and with clearly displayed capillaries ranging from 5-10 pixels in width. We compared our algorithm with an affine model, that accounts for pairwise rotation, scale, translation and shearing. The validation and segmentation procedures were controlled, so the same ROIs were used in both models. Both algorithms ran on the same machine, and both algorithms used the same local and global references to give a fair comparison. Figure 1(b) presents the comparison results of centreline error measure (CEM) between the outputs of the two algorithms. For fine structures, the affine model has on average 2-3 pixel misalignments and large error bars, up to 13-14 pixels. Our model, on the other hand, has a much more stable performance at 0.1-0.15 averaged pixel misalignment and no more than 0.3 pixel in all registered frames.

![Figure 1: (a) Temporal average $f_{\text{average}}$ of registered sequences (pre- and post- pulmonary cardiac bypass operation) for each patient (a total of 6 patients) (b) Top: CEM of registered sequences per patient from our algorithm; Bottom: CEM of registered sequences per patient using affine model. Note the different scales.](image)

Conclusions
In this paper, we first suggested a novel joint registration procedure with promising results in both the spatial and temporal domains. We then presented a novel pixel-wise wavelet scale-space approach for centreline segmentation without thresholding or region-growing, which is used for evaluation of registration accuracy. This allows comparison and non-invasive monitoring of fine-resolution microvasculature from an existing well-established technique. It provides the potential for detecting temporal changes in the circulation (possibly caused by microembolism) in real-time to allow for preventative measures to avoid aggravated blood-clotting impinging on patients’ quality of life and post-operative recovery.

References